
Multitask Learning and Benchmarking with Clinical Time Series Data

Challenging

- data is irregular in patient level but regular at local episode level
- time gap between two visits is random
- data for patient varies greatly in length
- absence of universally accepted benchmark

PROBLEM DEFINITION

➤ **Mortality:**

label indicates whether the patient died before hospital discharge

➤ **Decompensation:**

the target label indicates whether the patient will die within the next 24 hours

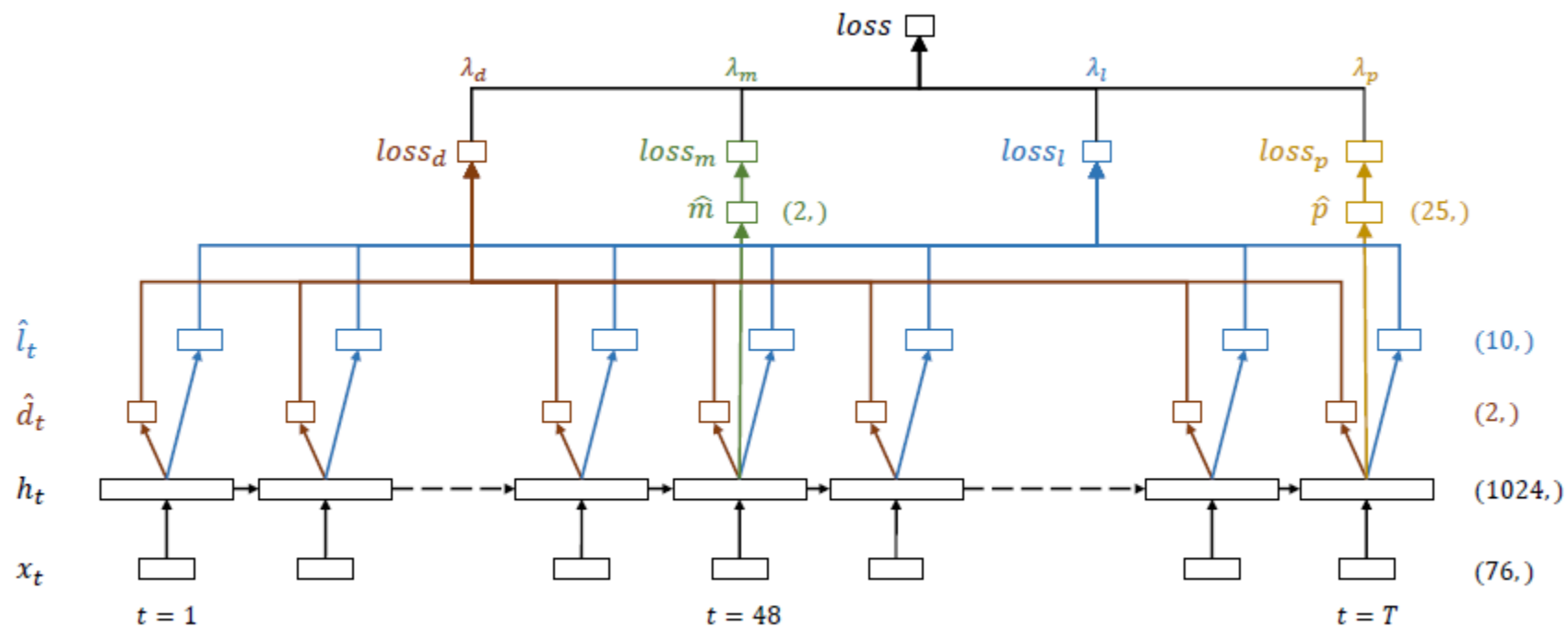
➤ **length of stay:**

Divide the range of value into ten buckets (0-1,1-2,...,7-8,8-14,14+)

➤ **Phenotype:**

25 conditions(12 critical conditions, 8 chronic conditions, 5 “mixed” conditions)

METHOD



METHOD

stay of length T hours, observations $\{x_t\}_{t \geq 1}$, x_t is vector of hour

mortality: $m \in \{0,1\}$ is single label indicating whether the patient die

decompensation: $\{d_t\}_{t \geq 1}^T$ where $d_t \in \{0,1\}$ is binary labels for each hour

length of stay: $\{l_t\}_{t \geq 1}^T$ where $l_t \in R$ is value number at each time step

Phenotyping: $p_{1:K} \in \{0,1\}^K$ is a vector of K binary phenotype labels

$$loss_d = \frac{1}{T} \sum_{t=1}^T CE(d_t, \hat{d}_t) \quad loss_p = \frac{1}{K} \sum_{k=1}^K CE(p_k, \hat{p}_k) \quad loss_l = \frac{1}{T} \sum_{t=1}^T MCE(l_{tk}, \hat{l}_{tk}) \quad loss_m = CE(m, \hat{m}) \quad loss_\ell = \frac{1}{T} \sum_{t=1}^T (\ell_t - \hat{\ell}_t)^2$$

$$loss_{mt} = \lambda_d \cdot loss_d + \lambda_l \cdot loss_l + \lambda_m \cdot loss_m + \lambda_p \cdot loss_p$$

RESULT

Model	AUROC	AUPRC	min(Se, +P)
Logistic regression	0.8442	0.4717	0.4693
LSTM	0.8540	0.5164	0.4905
Multitask LSTM	0.8550	0.4926	0.4745
Multitask LSTM*	0.8625	0.5169	0.4987

mortality

Model	Kappa	MSE	MAPE
Logistic regression	0.4021	63385	573.5
LSTM	0.4266	42165	235.9
Multitask LSTM	0.4258	42131	188.5

Length of stay

Model	AUROC	AUPRC	min(Se, +P)
Logistic regression	0.8704	0.2132	0.2688
LSTM	0.8946	0.2980	0.3438
Multitask LSTM	0.9004	0.3192	0.3484
Multitask LSTM**	0.9119	0.3322	0.3593

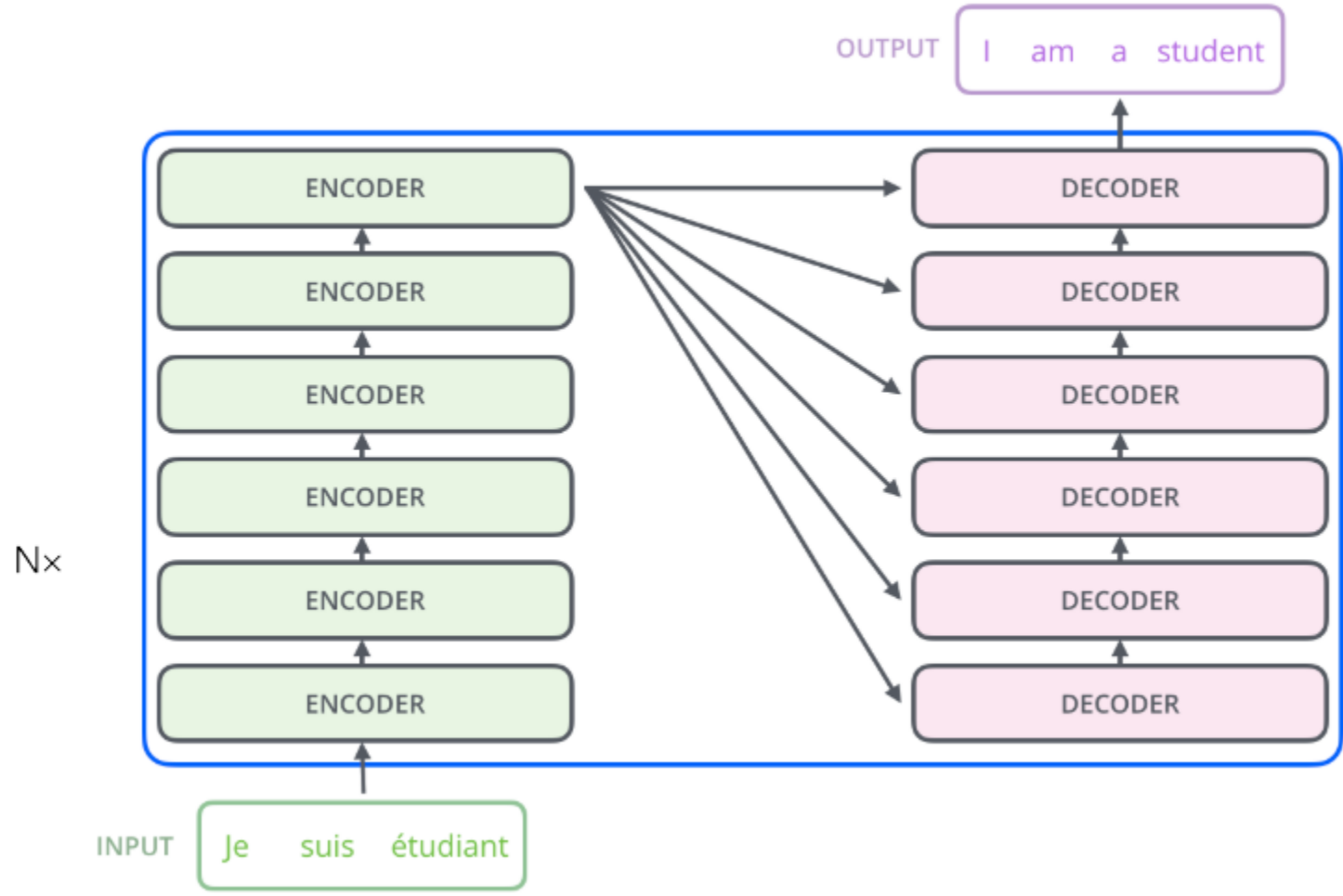
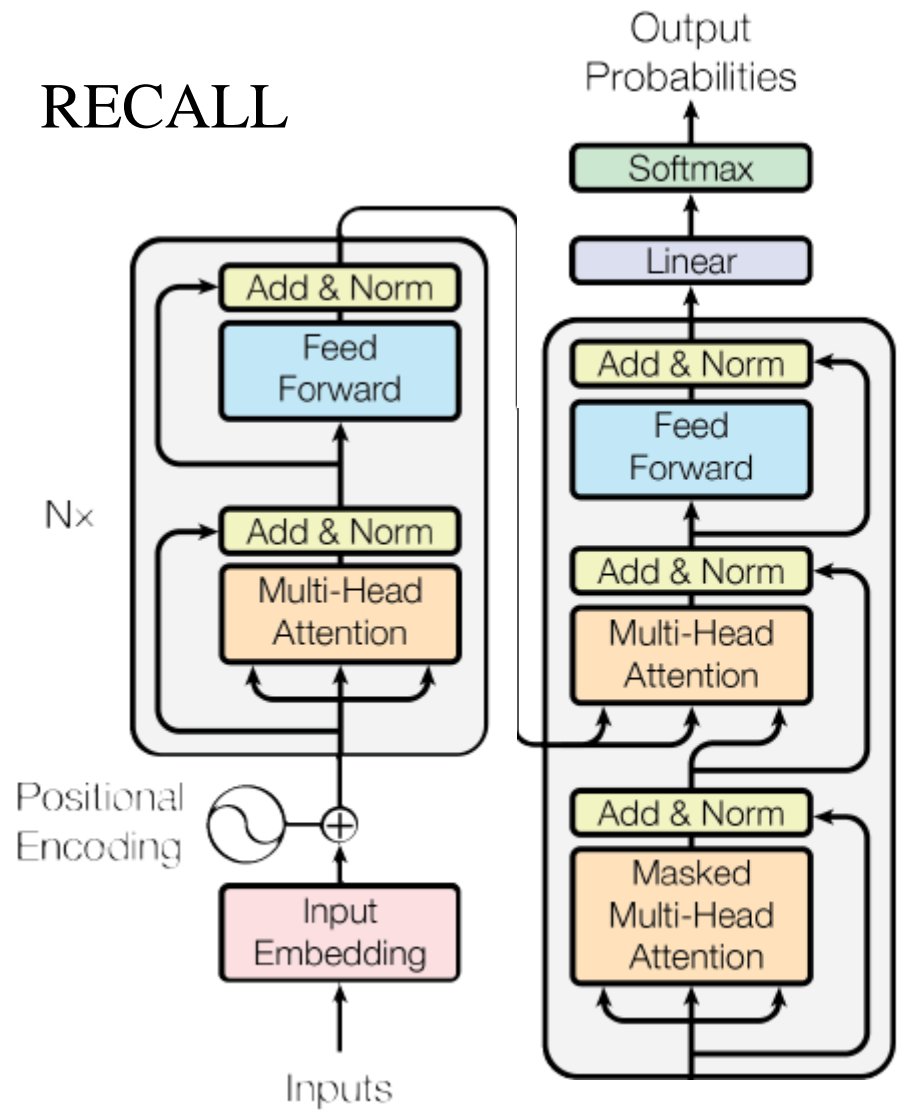
decompensation

Model	micro AUC	macro AUC	weighted AUC
Logistic regression	0.8007	0.7408	0.7320
1-layer LSTM	0.8206	0.7701	0.7573
2-layer LSTM	0.8213	0.7707	0.7587
Multitask LSTM	0.8174	0.7661	0.7533

phenotyping

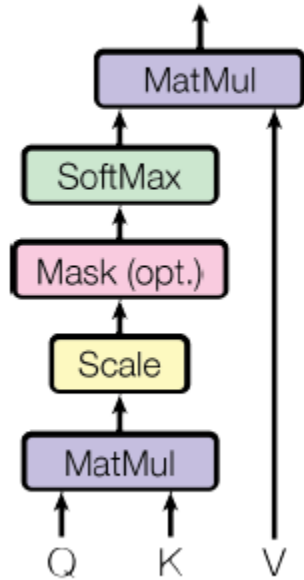
Attend and Diagnose:
Clinical Time Series Analysis Using Attention Models

RECALL



RECALL

Scaled Dot-Product Attention

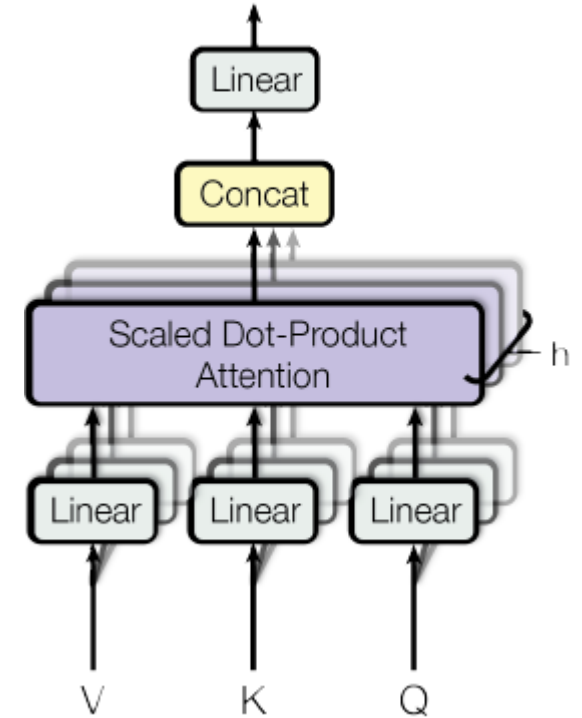


$$\text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)V$$

$$\text{MultiHead}(Q, K, V) = \text{Concat}(\text{head}_1, \dots, \text{head}_h)W^O$$

where $\text{head}_i = \text{Attention}(QW_i^Q, KW_i^K, VW_i^V)$

Multi-Head Attention



RECALL

Position-wise Feed-Forward Networks

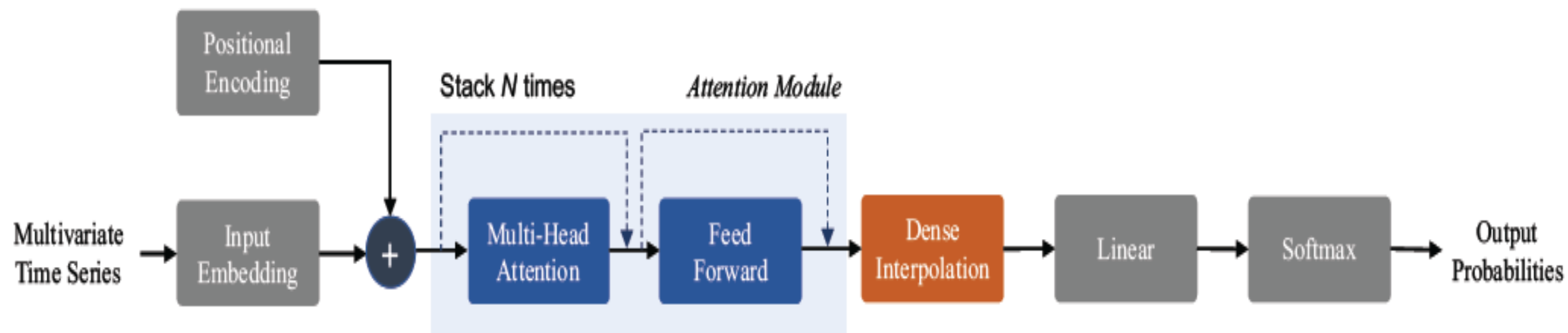
$$\text{FFN}(x) = \max(0, xW_1 + b_1)W_2 + b_2$$

Position Encoding

$$PE_{(pos, 2i)} = \sin(pos/10000^{2i/d_{\text{model}}})$$
$$PE_{(pos, 2i+1)} = \cos(pos/10000^{2i/d_{\text{model}}})$$

- Make use of the order of the sequence
- Inject some information about the relative or absolute position

METHOD



Attend and Diagnose: Clinical Time Series Analysis Using Attention Models

Ref : <http://jalammar.github.io/illustrated-transformer/>

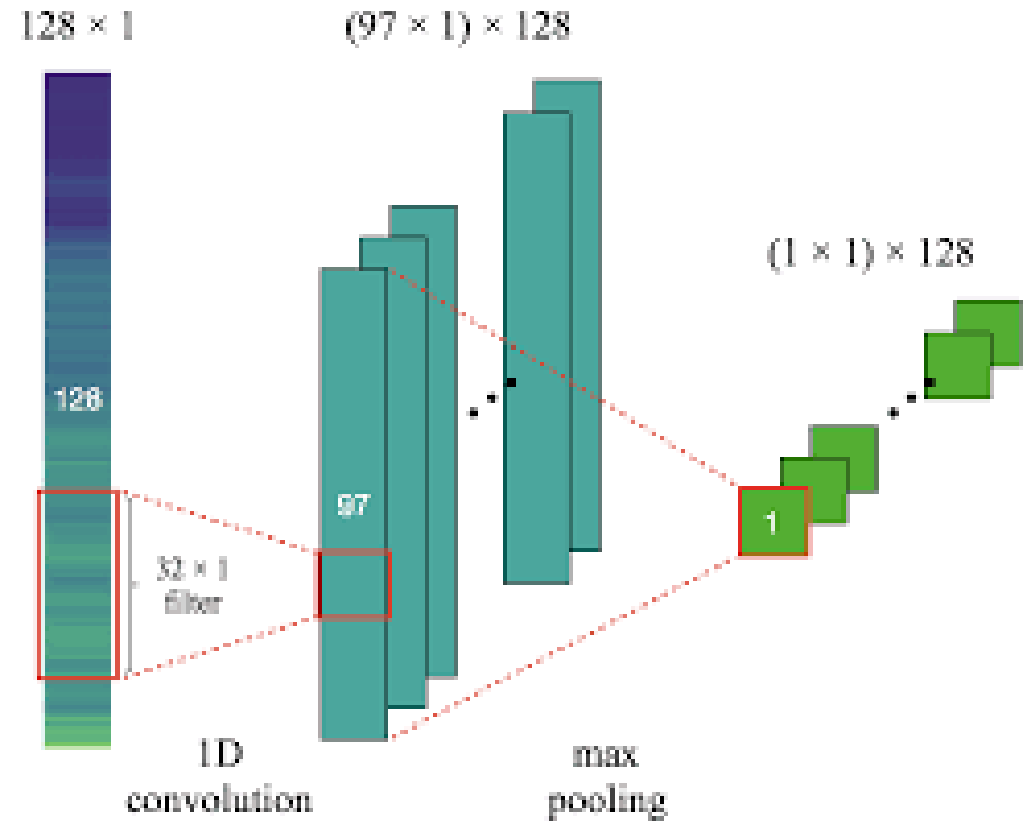
METHOD

Input Embedding

Conv1d captures the dependencies across different variables without considering the temporal information

Positional Embedding

adopt sin position embedding

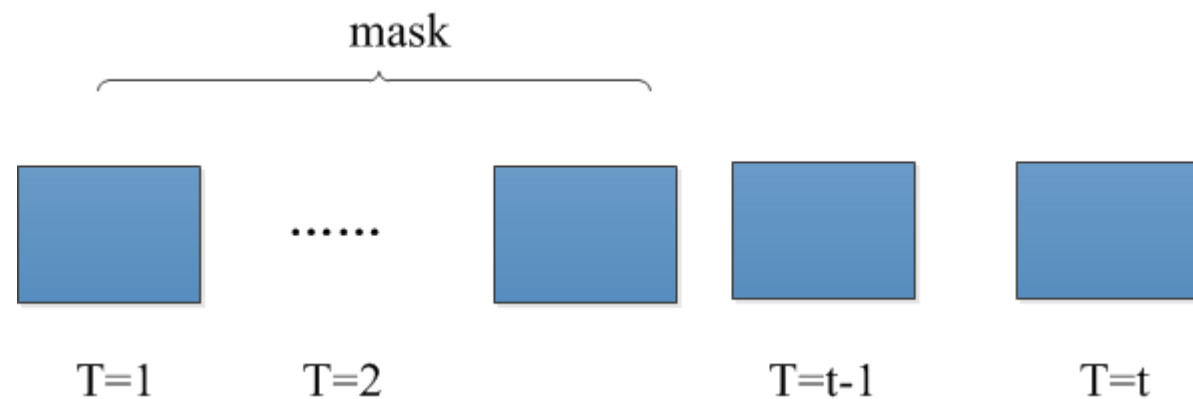
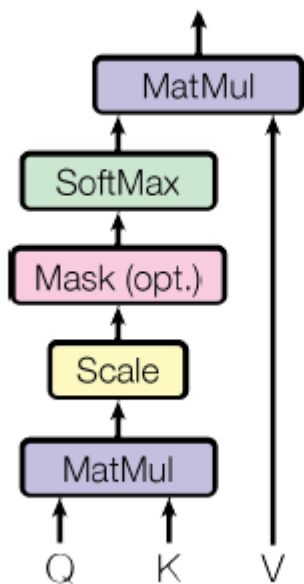


METHOD

Attention Module

Mask self-Attention

Scaled Dot-Product Attention



$$\text{Attention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \text{softmax}\left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d}}\right) \mathbf{V},$$

METHOD

Dense Interpolation for Encoding Order

Dense Interpolation Embedding

Input : Steps t of the time series and length of the sequence T , embeddings at step t as s_t , factor M .

Output: Dense interpolated vector representation u .

```
for  $t = 1$  to  $T$  do  
  |  $s = M * t / T$   
  | for  $m = 1$  to  $M$  do  
  | |  $w = \text{pow}(1 - \text{abs}(s - m) / M, 2)$   
  | |  $u_m = u_m + w * s_t$   
  | end  
end
```

Algorithm 1: Dense interpolation embedding with partial order for a given sequence.

Purpose : obtain sequence representation while preserving order

w denotes the contribution of s_t to the position m of the final vector representation u

METHOD

Linear and Softmax layers

Binary classification :

$$-(y \cdot \log(\hat{y})) + (1 - y) \cdot \log(1 - \hat{y})$$

Multi-label classification :

$$-(y \cdot \log(\hat{y})) + (1 - y) \cdot \log(1 - \hat{y})$$

Regression:

$$\sum_{t=1}^T (l_t - \hat{l}_t)^2$$

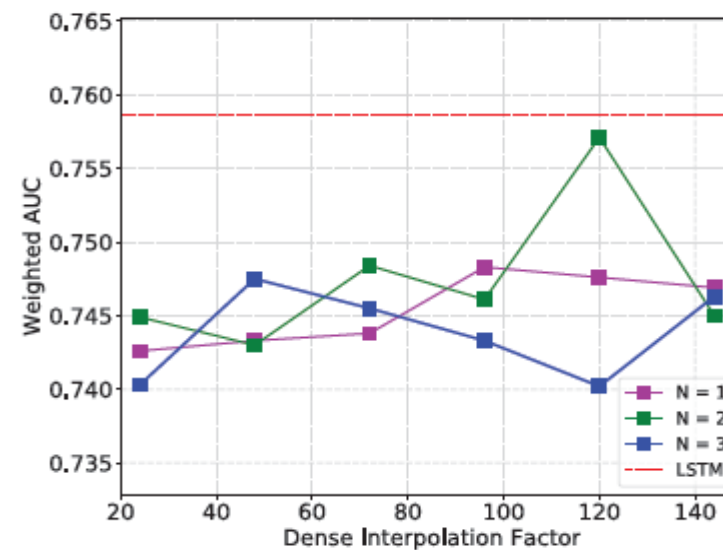
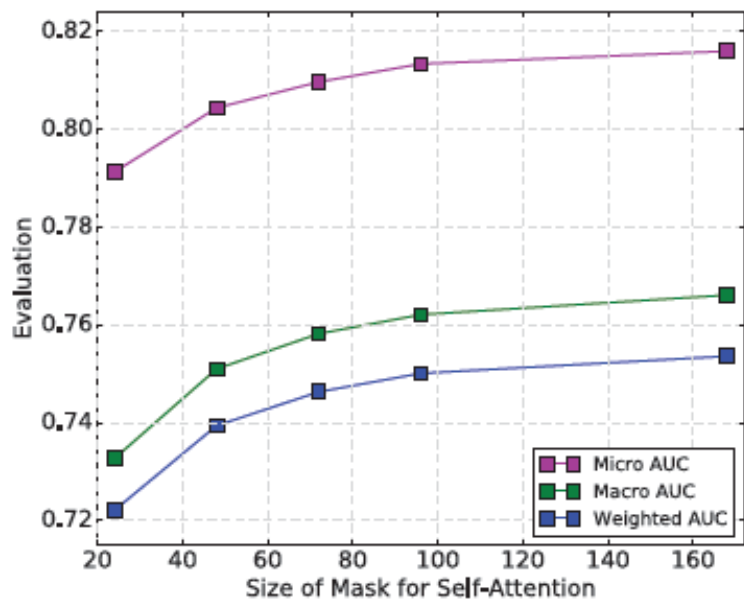
METHOD

Complexity Analysis

	Sequential operations	Complexity per Layer
RNN	$O(T)$	$O(T \cdot d^2)$
<i>SAnD</i>	$O(1)$	$O(T \cdot r \cdot d)$

RESULT

Phenotyping

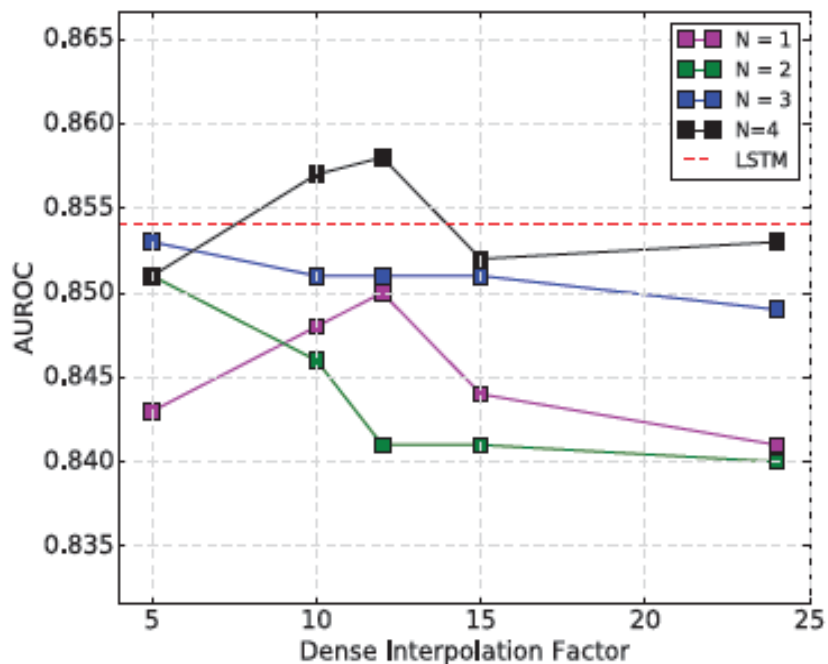


Attend and Diagnose: Clinical Time Series Analysis Using Attention Models

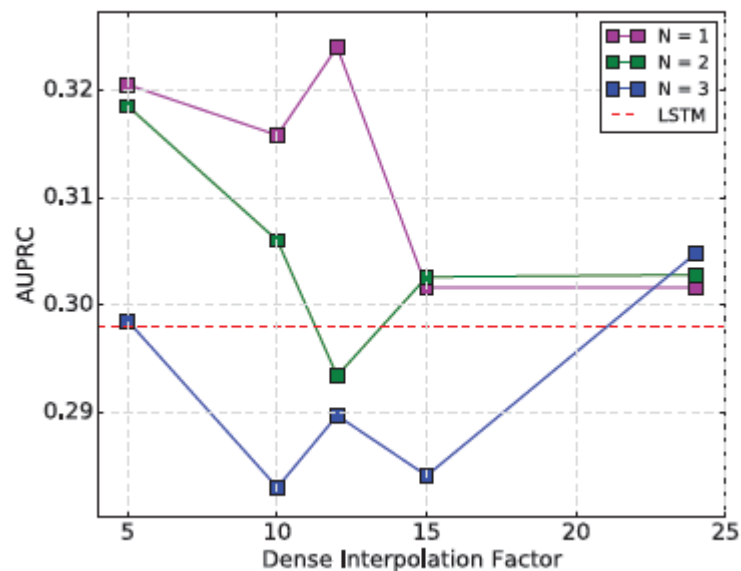
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RESULT

Mortality

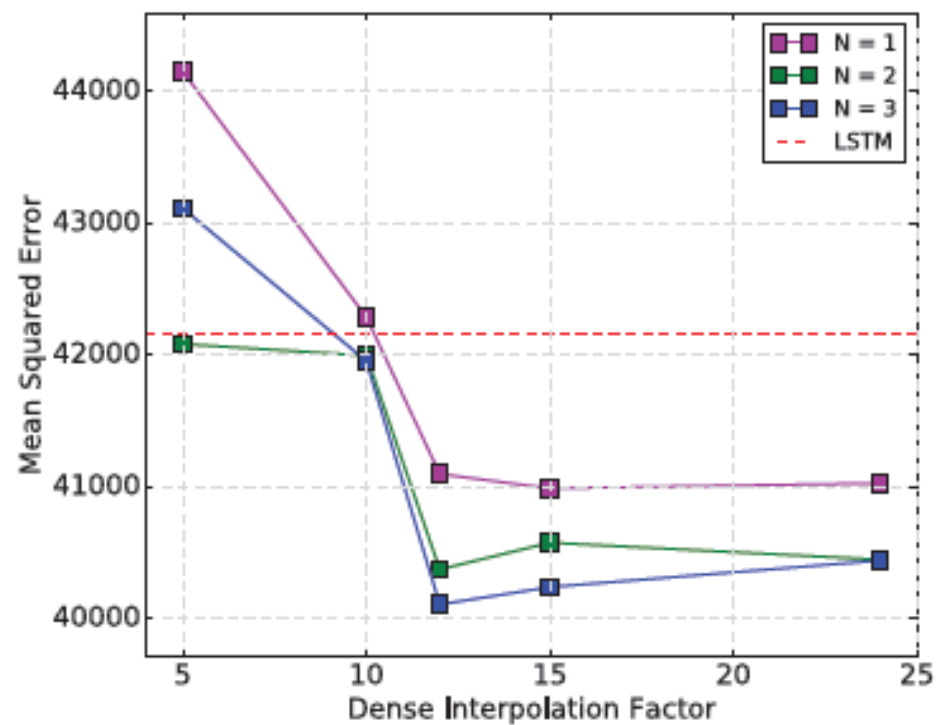


Decompensation



RESULT

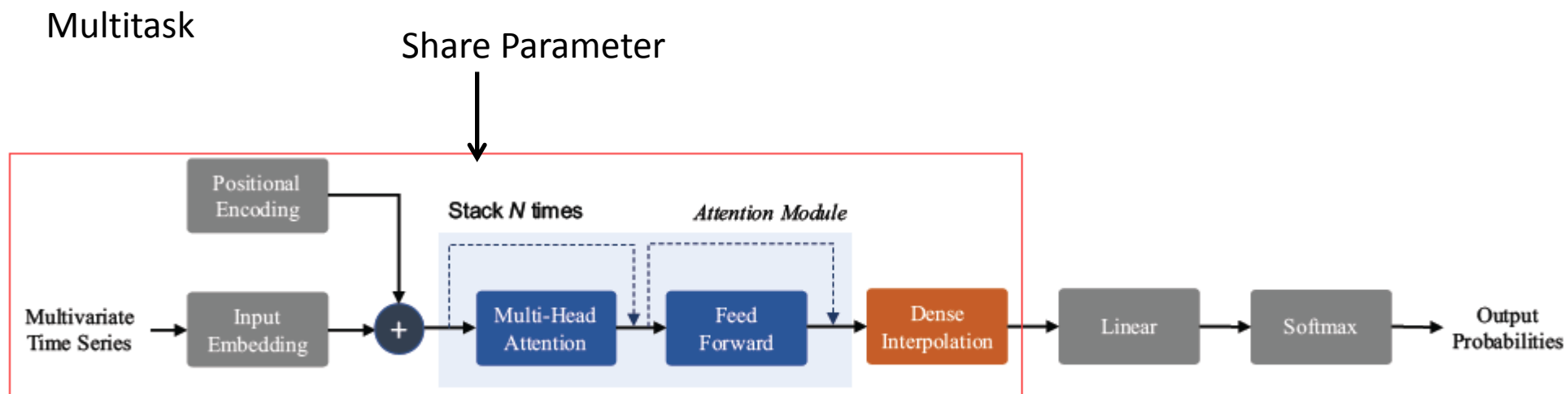
Length of Stay



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RESULT



$$\ell_{mt} = \lambda_p \ell_{ph} + \lambda_{il} \ell_{ihm} + \lambda_d \ell_{dc} + \lambda_l \ell_{los},$$

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RESULT

Metrics	Method				
	LR	LSTM	<i>SAnD</i>	LSTM-Multi	<i>SAnD</i> -Multi
Task 1: Phenotyping					
Micro AUC	0.801	0.821	0.816	0.817	0.819
Macro AUC	0.741	0.77	0.766	0.766	0.771
Weighted AUC	0.732	0.757	0.754	0.753	0.759
Task 2: In Hospital Mortality					
AUROC	0.845	0.854	0.857	0.863	0.859
AUPRC	0.472	0.516	0.518	0.517	0.519
min(Se, P+)	0.469	0.491	0.5	0.499	0.504
Task 3: Decompensation					
AUROC	0.87	0.895	0.895	0.900	0.908
AUPRC	0.2132	0.298	0.316	0.319	0.327
min(Se, P+)	0.269	0.344	0.354	0.348	0.358
Task 4: Length of Stay					
Kappa	0.402	0.427	0.429	0.426	0.429
MSE	63385	42165	40373	42131	39918
MAPE	573.5	235.9	167.3	188.5	157.8

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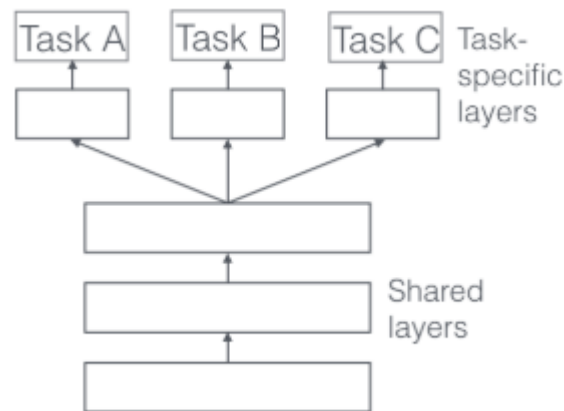
Appendix

➤ Hard parameter sharing

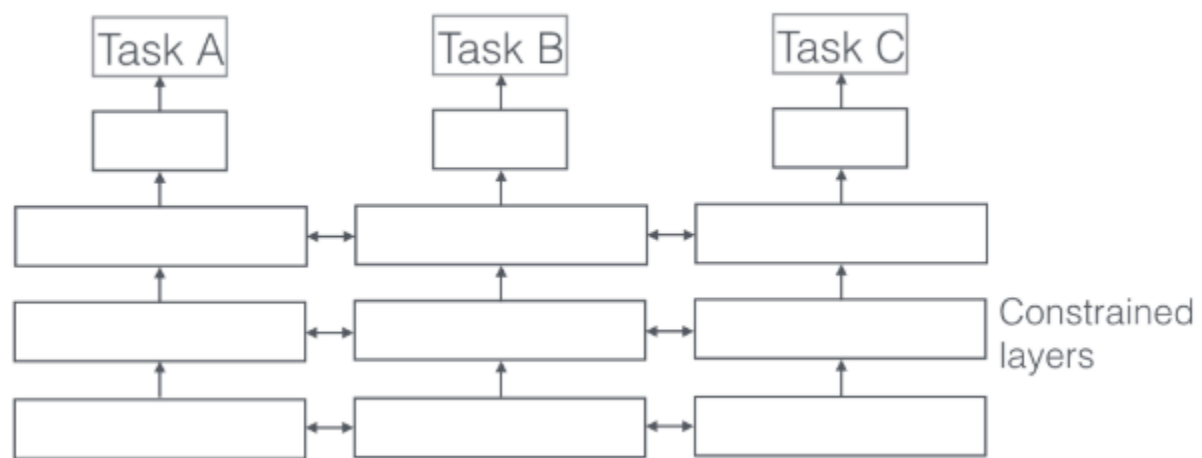
share the hidden layers between all tasks, while keeping several task-specific output layers

➤ Soft parameter sharing

each task has its own model with its own parameters, but train jointly



Hard Parameter Sharing



Soft Parameter Sharing

THANK YOU
